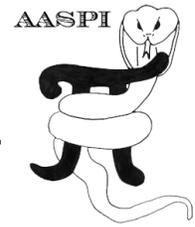


Spectral Attributes: Program **spec_clssa**

CONSTRAINED LEAST-SQUARES SPECTRAL ANALYSIS -
PROGRAM spec_clssa



Alternative Spectral Decomposition Algorithms

Spectral decomposition methods can be divided into three classes: those that use quadratic forms, those that use linear forms and those that use atom decomposition. Quadratic forms are based on Wigner-Ville distribution, which can be easily designed but lose the phase component of the data and therefore cannot be used in reconstruction. Linear forms are based on short time Fourier transform (STFT), and include the S transform and the continuous wavelet transform (or CWT) as in program **spec_cwt**. Program **spec_clssa** is a nonlinear implementation of the short time Fourier transform. Atomic decomposition reconstructs the signal by using small “atom-sized” signals (in our case wavelets), such as complex matching pursuit (program **spec_cmp**) and the Hilbert-Huang transform.

spec_clssa computation flow chart

While there is only one input file to program **spec_clssa**, there are many output files which can easily fill your disk drives. Detailed spectral analysis will typically be done about a reservoir or other zone of interest, such that the input data volume may be windowed. If this is not the case, it is best to first run several of the statistical summary volumes including the peak magnitude, peak frequency, and peak phase, and phase residue entire volume. These spectra may be sufficient for your analysis. If not, the peak frequency volume will serve as a guide as to which spectral components are well tuned.

Spectral Attributes: Program **spec_clssa**

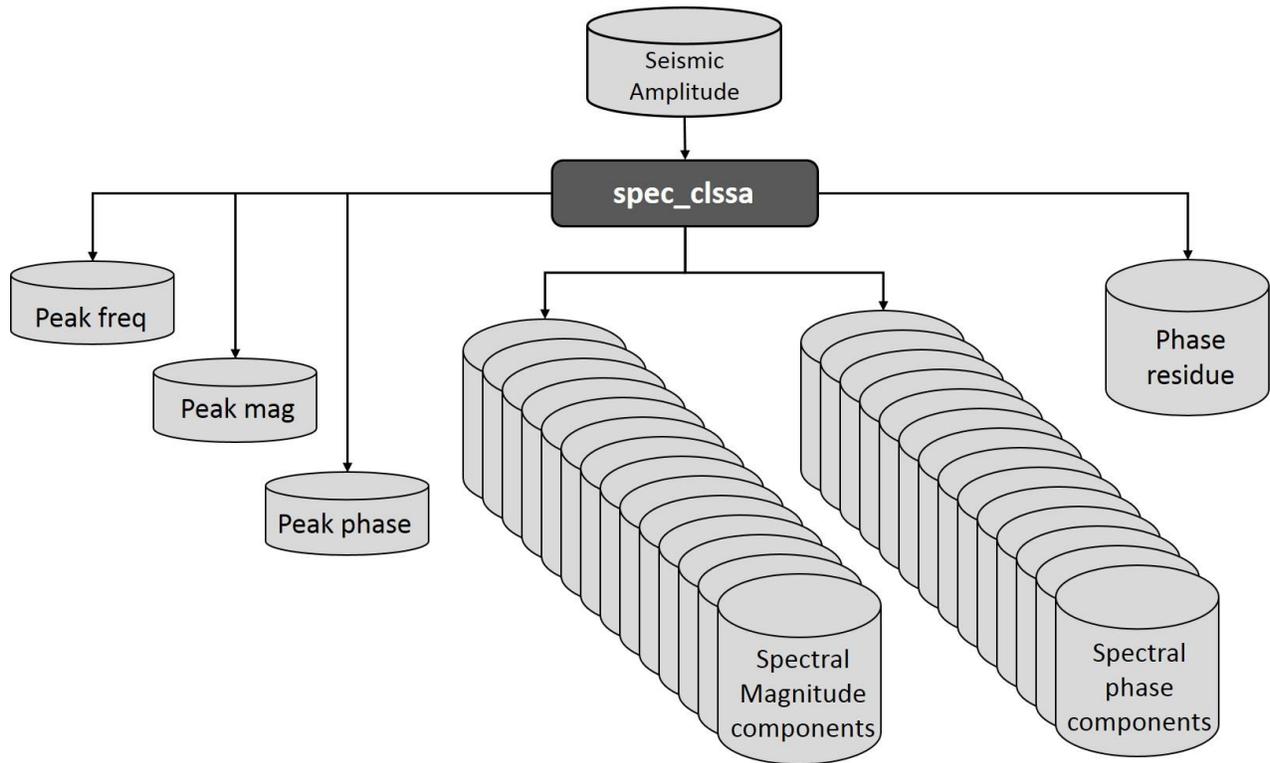
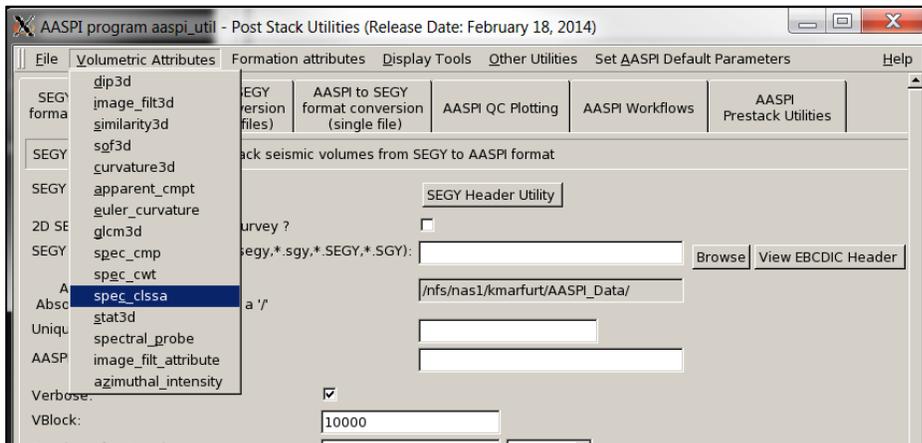


Figure 1. The flow chart for program **spec_clssa** – constrained least-squares spectral analysis.

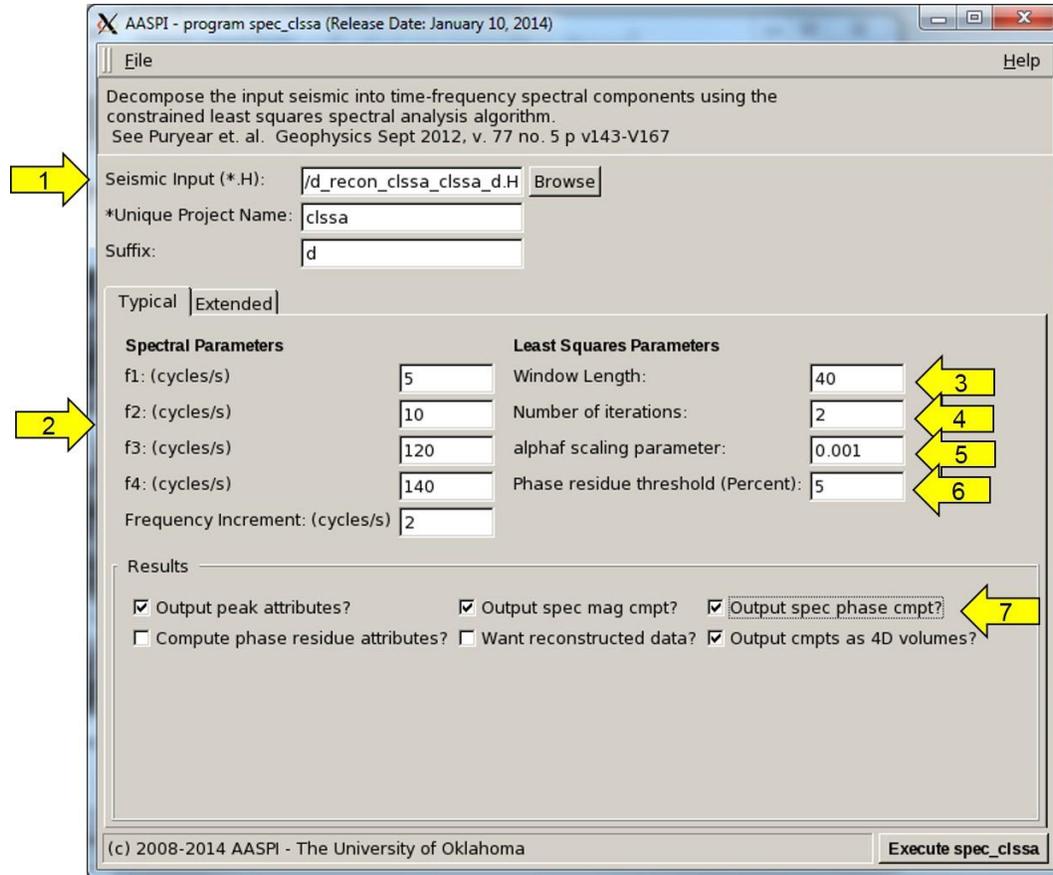
Computing spectral components

To begin, click the *Volumetric Attributes* tab in the **aaspi_util** window and select the program **spec_clssa** :



Spectral Attributes: Program `spec_clssa`

Program `spec_clssa` performs spectral decomposition using a constrained least-squares spectral analysis method. The following window appears:



You will note that many of the attributes appear to be similar to those of program `spec_cmp`, spectral decomposition using a complex matching pursuit algorithm. First, enter the (1) the name of the *Seismic Input (*.H)* file you wish to decompose, as well as a *Unique Project Name* and *Suffix* as you have done for other AASPI programs.

Constrained least-squares spectral analysis (clssa)

Puryear et al. (2012) proposed an inversion-based algorithm for computing the time frequency analysis of reflection seismograms using constrained least-squares spectral analysis. The method resulted in spectra that have reduced window smearing for a given window length relative to the discrete Fourier transform irrespective of window shape, and a time-frequency analysis with a combination of time and frequency resolution that is superior to the short time Fourier transform and the continuous wavelet transform. As compared with the continuous wavelet transform, the method has improved temporal resolution, particularly at low frequencies.

Spectral Attributes: Program **spec_clssa**

Seismic spectral decomposition is a trace-by-trace operation. Because each 1D seismic trace is converted to a 2D time-frequency panel, the process expands the dimensions of the original data via a non-unique transformation, suggesting an inversion-based approach to the problem. Several investigators have used different empirical criteria to define inversion-based spectral analysis methods. Following the Portniaguine and Castagna (2004) approach to seismic wavelet decomposition and reflectivity inversion, we invert the normal equations by applying an iteratively reweighted least-squares regularization algorithm to the complex spectral decomposition inverse problem as described in the box “Mathematical Implementation”.

Mathematical Implementation

Start with the definition of the forward problem.

$$\mathbf{F}\mathbf{m} = \mathbf{d} , \quad (\text{A1})$$

where \mathbf{F} is the kernel matrix composed of complex sinusoidal basis functions,

$$F_{nk} = \exp[i(2\pi k \Delta f n \Delta t)] = \cos(2\pi k \Delta f n \Delta t) + i \sin(2\pi k \Delta f n \Delta t) , \quad (\text{A2})$$

$m_k = m(2\pi k \Delta f)$ is the model parameter vector (i.e. the desired spectral coefficients), and $d_n = d(n \Delta t)$ is the windowed seismic amplitude data. Forming the normal equations by multiplying both sides of equation A1 by \mathbf{F}^H , the complex conjugate or Hilbert transpose of \mathbf{F} , gives

$$\mathbf{F}^H \mathbf{F} \mathbf{m} = \mathbf{F}^H \mathbf{d} . \quad (\text{A3})$$

The objective of the inverse problem is to compute \mathbf{m} given \mathbf{F} and \mathbf{d} . The classical least-squares solution to equation A1 is then

$$\mathbf{m} = (\mathbf{F}^H \mathbf{F})^{-1} \mathbf{F}^H \mathbf{d} . \quad (\text{A4})$$

Conventional Fourier transforms used in filtering are constructed to be orthogonal, such that $\mathbf{F}^H \mathbf{F} = \mathbf{I}$, where \mathbf{I} is the identity matrix. In this case, equation A4 reduces to

$$\mathbf{m} = \mathbf{F}^H \mathbf{d} , \quad (\text{A5})$$

which is equivalent to the discrete Fourier transform of the windowed trace segment. If the analysis window is $T=0.1$ s, orthogonality requires $\Delta f = 1/T = 10$ Hz. If we wish to estimate intermediate spectral components at a 2 Hz interval, we need to use the more general equation A4. A finer frequency increment results an underdetermined system with more unknowns than equations. We constrain the inversion by introducing two diagonal matrices. The data weight matrix, \mathbf{W}_d , acts as a taper, where smaller weights at the window edges provides for greater tolerance of the misfit. In contrast, the model weight matrix, \mathbf{W}_m , change iteratively, in general favoring the strongest spectral components, and attenuating the corresponding weaker aliases. Applying \mathbf{W}_m and \mathbf{W}_d to equation A1,

$$\mathbf{W}_d \mathbf{F} \mathbf{W}_m (\mathbf{W}_m)^{-1} \mathbf{m} = \mathbf{W}_d \mathbf{d} , \quad (\text{A6})$$

we introduce the weighted quantities

$$\mathbf{F}_w = \mathbf{W}_d \mathbf{F} \mathbf{W}_m \text{ and } \mathbf{m}_w = \mathbf{W}_m^{-1} \mathbf{m} , \quad (\text{A6})$$

and then recast equation A5 as a model and data-weighted ill-posed inverse problem:

$$\mathbf{F}_w \mathbf{m}_w = \mathbf{W}_d \mathbf{d} . \quad (\text{A7})$$

To solve equation A7, we add regularization:

$$\min \varepsilon^2 = \|\mathbf{F}_w \mathbf{m}_w - \mathbf{W}_d \mathbf{d}\|^2 + \alpha \|\mathbf{m}_w\|^2 \quad (\text{A8})$$

where α is a regularization parameter that can be varied to control the sparsity and stability of the solution. Note that if \mathbf{W}_m is proportional to \mathbf{m} , small values of \mathbf{m} become large values of \mathbf{m}_w which are then minimized, giving us a sparse solution. Using an analytical Lagrange solution to equation A8, we solve first for the weighted model parameters

$$\mathbf{m}_w = \mathbf{F}_w^H (\mathbf{F}_w \mathbf{F}_w^H + \alpha \mathbf{I})^{-1} \mathbf{W}_d \mathbf{d} , \quad (\text{A9})$$

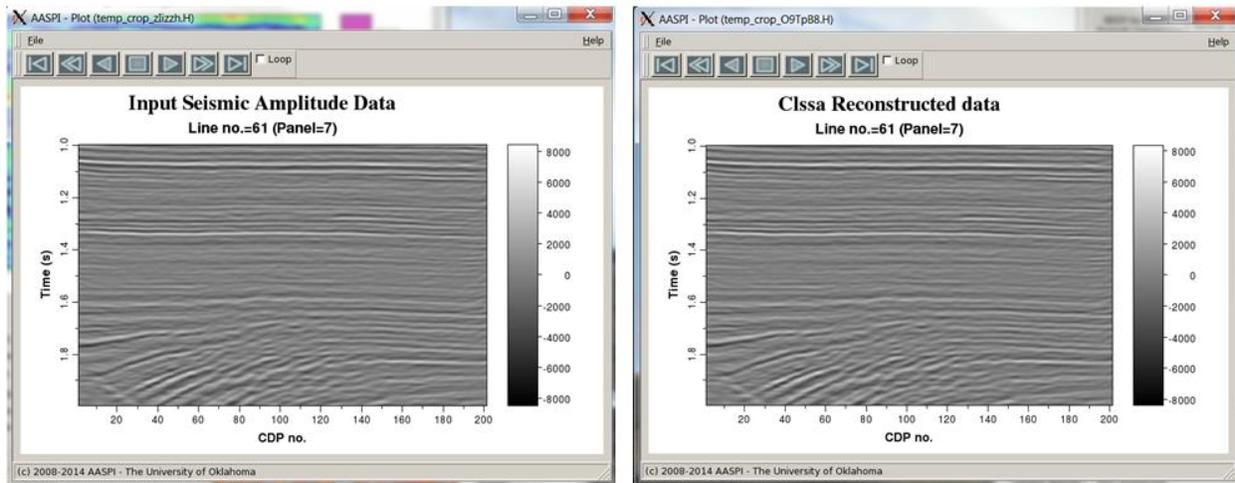
followed by reconstruction

$$\mathbf{m} = \mathbf{W}_m \mathbf{m}_w . \quad (\text{A10})$$

Values of α are chosen to be a percentage of $\|\mathbf{F}_w \mathbf{F}_w^H\|$. Portniaguine and Castagna (2004) find the CLSSA utilizing a real basis function to be not quite as good as using a complex basis function, but better than the conventional DFT. This is significant because CLSSA using only the real waveform has precisely the same temporal resolution as the Fourier transform while having greatly improved frequency resolution. This indicates that, for a given window, CLSSA has a better Heisenberg uncertainty product (standard deviation of the waveform in time multiplied by the standard deviation of the spectrum) than does the Fourier transform. Thus far, they have not found a window for which this is not the case.

Spectral Attributes: Program `spec_clssa`

The *Reconstruction parameters* (2) indicates the four corner frequencies f_1 , f_2 , f_3 , and f_4 used to reconstruct the seismic data after flattening. A raised-cosine taper is applied between f_1 and f_2 as well as between f_3 and f_4 . The choice of frequency increment and range does not significantly impact the decomposition time, only the output size of the data if you choose to output either spectral magnitude or spectral phase components as either a sequence of constant frequency volumes or as an equivalent 4D volume. In this example we used a 40 ms window, which implies a frequency resolution of $\Delta f = 1/0.040 \text{ s} = 25 \text{ Hz}$ is necessary to reconstruct the data using a DFT. Using this argument, we can say that the spectra is oversampled, which is validated by the excellent reconstruction on the right.



The (3) *Window length* indicates the length of the time window function used in spectral decomposition. As discussed above, the CLSSA algorithm is focused on solving an inverse problem. The window length parameter determines how long the inverse operator would cover, which can affect the time-frequency resolution. As an iterative method, the (4) *Number of iterations* defines the number of iterations used in iteratively reweighted least-squares solution. A larger number of iterations provides a more-accurate least-squares approximation, but also consumes more time. The (5) *alpha f scaling parameter* is the regularization parameter α in equations A8 and A9 above, which stabilizes the least-squares regression process.

The (6) *Phase residue threshold (Percent)* limits the phase residue attribute computation. When it is larger, more phase residue will appear corresponding to weaker events.

The Phase Residue

Ghiglia and Pritt (1998) provide an excellent survey of 2D phase-unwrapping techniques and show how a complex residue theorem based on vector calculus can be applied to the phase-unwrapping problem. They use a rectangular integration path aligned with the t and f axes. We choose a smaller diamond-shaped integration path about each sample $(j\Delta t, k\Delta f)$ given by

$$I_{jk} = \frac{W[\psi(t_{j-1}, f_k) - \psi(t_j, f_{k-1})]}{2\pi} + \frac{W[\psi(t_j, f_{k-1}) - \psi(t_{j+1}, f_k)]}{2\pi} + \frac{W[\psi(t_{j+1}, f_k) - \psi(t_j, f_{k+1})]}{2\pi} + \frac{W[\psi(t_j, f_{k+1}) - \psi(t_{j-1}, f_k)]}{2\pi} \quad (\text{B1})$$

where ψ is the phase and W is a wrapping operator that produces an output that falls between $\pm\pi$. If the integral I_{jk} in equation B1 is nonzero, there are inconsistent phase points, which Ghiglia and Pritt (1998) call “phase residues”. The figure below shows how the residue is calculated for a small portion of a typical wrapped time-frequency phase matrix. Area A is continuous, with a phase residue = 0.0, while area B is discontinuous with a phase residue = 1.0 .

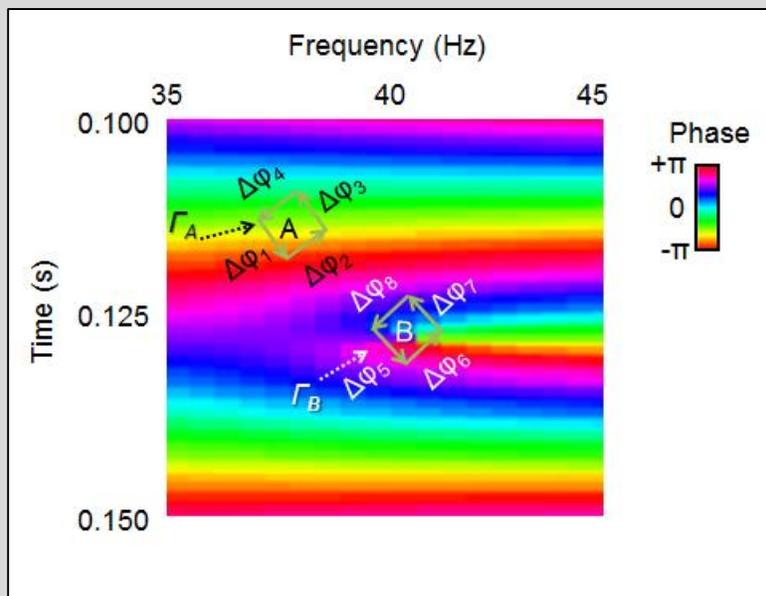


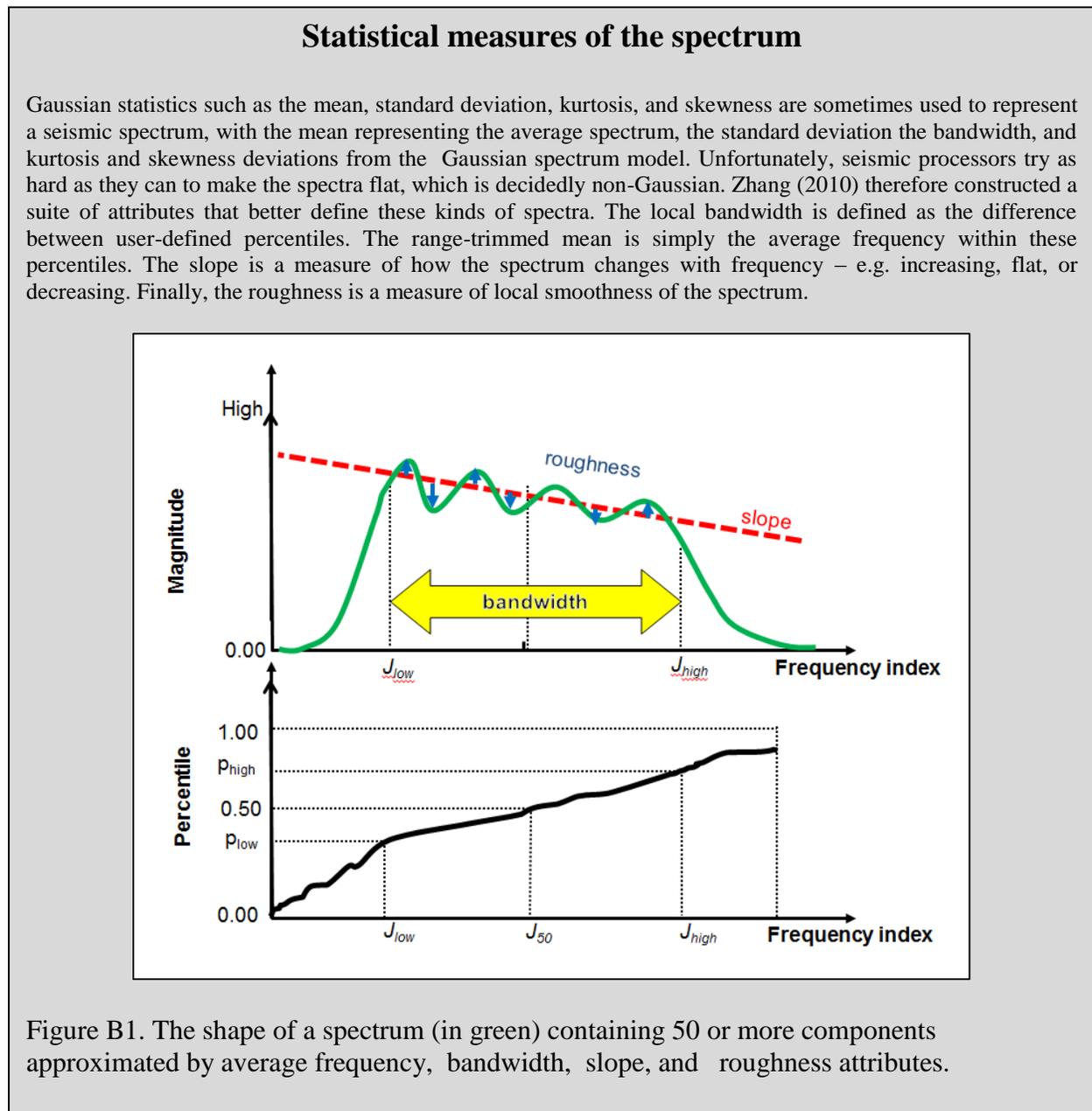
Figure B1. Line integrals about analysis points A and B used to compute the phase residue.

Matos et al. (2011) find phase attributes are sensitive to the same kinds of stratigraphic discontinuities seen by analyzing the magnitude component of time-frequency distribution using wavelet transforms and the continuous wavelet transform. Because phase is often a more seismic measure than magnitude, it holds significant promise in mapping stratigraphic unconformities.

Accurate computation of phase residues requires relatively fine sampling across frequency. We suggest setting the computational $\Delta f=1$ Hz. Unfortunately, if you do this and choose to output these many components as well, you may fill up your disk drive. To analyze individual components we suggest a coarser output $\Delta f=5$ Hz for subsequent loading into your interpretation workstation.

Statistical measures of the spectrum

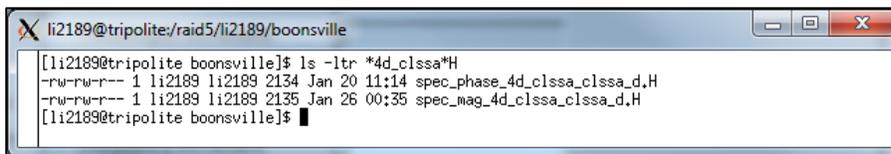
Like program `spec_cmp`, program `spec_clssa` provides several statistical measures of the spectrum that can be used in addition to or in place of the full 4D spectral components. The peak spectral magnitude, peak spectral frequency, and peak spectral phase are easy to understand. You obtain these by placing a checkmark in front of *Want peak attributes?*



Spectral Attributes: Program `spec_clssa`

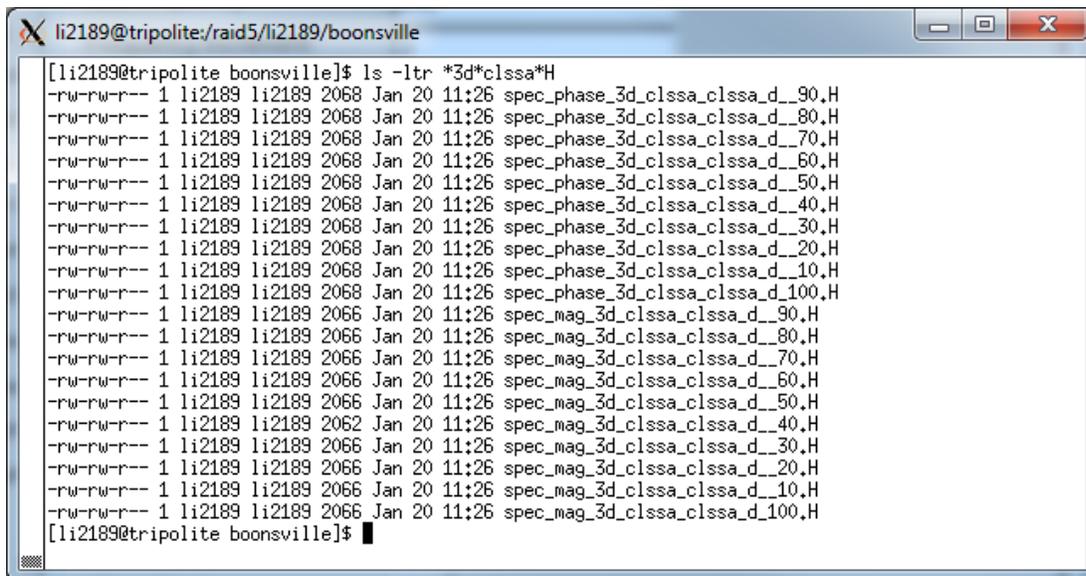
Individual spectral components

If you place a checkmark in front of *Want spec mag cmpt?* or *Want spec phase cmpt?*, you will obtain each of the spectral components that range between f_1 and f_4 with the desired *Frequency Increment*. For interpretation of the components on most interpretation workstations, it may be easier to load these components separately. If you place a check mark in front of (9) *Store cmpts as 4D cubes?*, you obtain spectral gathers that are ordered with the time axis running fastest, followed by the frequency axis, (such that the first two indices represent a time-frequency distribution) followed by the CDP numbers (inline axis) and line numbers (crossline axis). The 4D volumes will have the following names for this job:



```
li2189@tripolite/raid5/li2189/boonsville
[[li2189@tripolite boonsville]$ ls -ltr *4d_clssa*H
-rw-rw-r-- 1 li2189 li2189 2134 Jan 20 11:14 spec_phase_4d_clssa_clssa_d.H
-rw-rw-r-- 1 li2189 li2189 2135 Jan 26 00:35 spec_mag_4d_clssa_clssa_d.H
[[li2189@tripolite boonsville]$
```

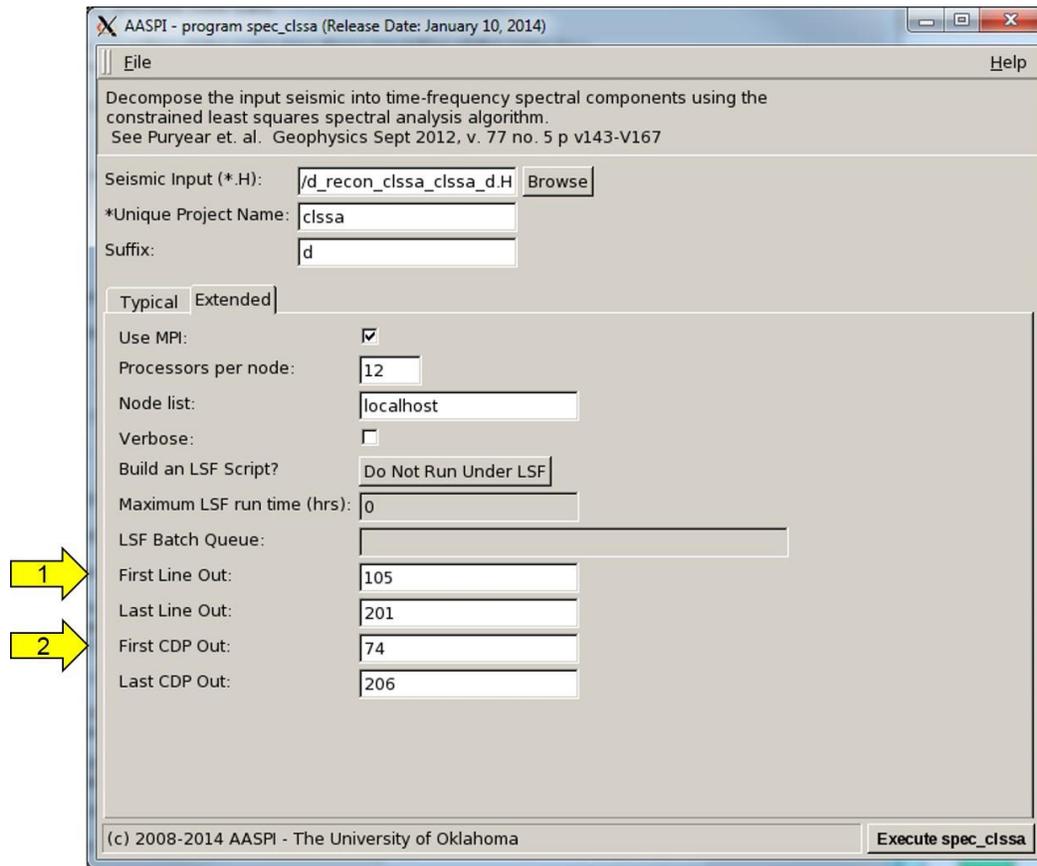
If you ask for spectral components not to be stored as a 4D cube the constant-frequency 3D spectral magnitude and spectral phase volumes will have the frequency value encoded in the file name:



```
li2189@tripolite/raid5/li2189/boonsville
[[li2189@tripolite boonsville]$ ls -ltr *3d*clssa*H
-rw-rw-r-- 1 li2189 li2189 2068 Jan 20 11:26 spec_phase_3d_clssa_clssa_d_90.H
-rw-rw-r-- 1 li2189 li2189 2068 Jan 20 11:26 spec_phase_3d_clssa_clssa_d_80.H
-rw-rw-r-- 1 li2189 li2189 2068 Jan 20 11:26 spec_phase_3d_clssa_clssa_d_70.H
-rw-rw-r-- 1 li2189 li2189 2068 Jan 20 11:26 spec_phase_3d_clssa_clssa_d_60.H
-rw-rw-r-- 1 li2189 li2189 2068 Jan 20 11:26 spec_phase_3d_clssa_clssa_d_50.H
-rw-rw-r-- 1 li2189 li2189 2068 Jan 20 11:26 spec_phase_3d_clssa_clssa_d_40.H
-rw-rw-r-- 1 li2189 li2189 2068 Jan 20 11:26 spec_phase_3d_clssa_clssa_d_30.H
-rw-rw-r-- 1 li2189 li2189 2068 Jan 20 11:26 spec_phase_3d_clssa_clssa_d_20.H
-rw-rw-r-- 1 li2189 li2189 2068 Jan 20 11:26 spec_phase_3d_clssa_clssa_d_10.H
-rw-rw-r-- 1 li2189 li2189 2068 Jan 20 11:26 spec_phase_3d_clssa_clssa_d_100.H
-rw-rw-r-- 1 li2189 li2189 2066 Jan 20 11:26 spec_mag_3d_clssa_clssa_d_90.H
-rw-rw-r-- 1 li2189 li2189 2066 Jan 20 11:26 spec_mag_3d_clssa_clssa_d_80.H
-rw-rw-r-- 1 li2189 li2189 2066 Jan 20 11:26 spec_mag_3d_clssa_clssa_d_70.H
-rw-rw-r-- 1 li2189 li2189 2066 Jan 20 11:26 spec_mag_3d_clssa_clssa_d_60.H
-rw-rw-r-- 1 li2189 li2189 2066 Jan 20 11:26 spec_mag_3d_clssa_clssa_d_50.H
-rw-rw-r-- 1 li2189 li2189 2062 Jan 20 11:26 spec_mag_3d_clssa_clssa_d_40.H
-rw-rw-r-- 1 li2189 li2189 2066 Jan 20 11:26 spec_mag_3d_clssa_clssa_d_30.H
-rw-rw-r-- 1 li2189 li2189 2066 Jan 20 11:26 spec_mag_3d_clssa_clssa_d_20.H
-rw-rw-r-- 1 li2189 li2189 2066 Jan 20 11:26 spec_mag_3d_clssa_clssa_d_10.H
-rw-rw-r-- 1 li2189 li2189 2066 Jan 20 11:26 spec_mag_3d_clssa_clssa_d_100.H
[[li2189@tripolite boonsville]$
```

There are several 'expert' controls under the *Extended* tab:

Spectral Attributes: Program `spec_clssa`



Since the amount of output can be quite large, it may be useful to run `spec_clssa` on only a limited range of (1) inlines and (2) crosslines.

You will probably want to experiment with these parameters a bit to calibrate them for the kind of data your encounter. It is reasonable to expect that most surveys of a similar vintage from the Gulf of Mexico will have similar spectral ranges and signal-to-noise ratios. Likewise, similar surveys acquired in the Permian Basin of west Texas will be similar to each other. In order to simplify parameter choices, In order to simplify parameter choices, you can then `cat` AASPI “.parms” file to examine its content or set it to your desired default parameters:

Spectral Attributes: Program `spec_clssa`

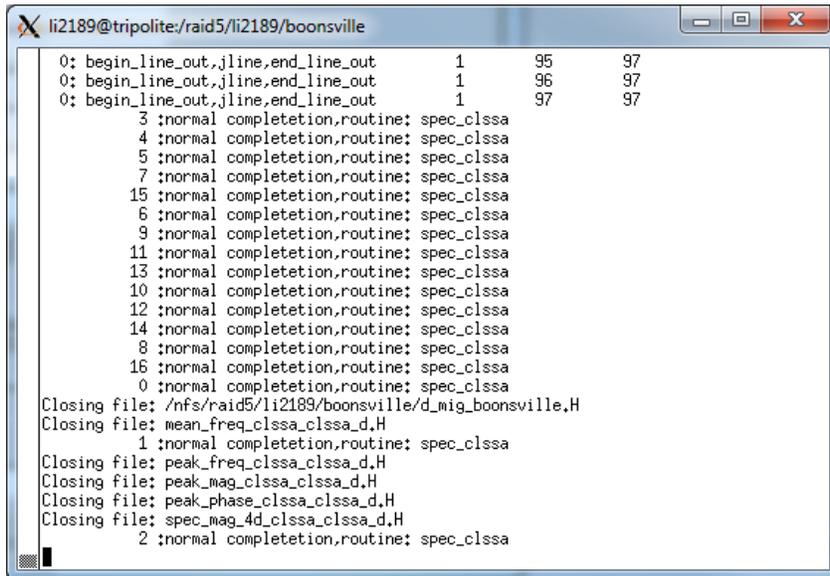


```
li2189@tripolite:raid5/li2189/boonsville
[li2189@tripolite boonsville]$ cat spec_clssa.parms
input_fn="/nfs/raid5/li2189/boonsville/d_mig_boonsville,H"
inline_dip_fn=""
crossline_dip_fn=""
error_fn="spec_clssa_clssa_d,err"
output_fn="spec_clssa_clssa_d,out"
avg_spec_power_fn="avg_spec_power_clssa_clssa_d,H"
avg_spec_power_scale_fn="avg_spec_power_scale_clssa_clssa_d,H"
avg_spec_unwrapped_phase_fn="avg_unwrapped_phase_clssa_clssa_d,H"
modeled_fn=""
residual_fn=""
d_recon_fn=""
spec_mag_3d_fn=""
spec_mag_4d_fn="spec_mag_4d_clssa_clssa_d,H"
spec_phase_3d_fn=""
spec_phase_4d_fn=""
spec_voice_3d_fn=""
spec_voice_4d_fn="spec_voice_4d_clssa_clssa_d,H"
phase_residue_mag_fn=""
phase_residue_freq_fn=""
peak_mag_fn="peak_mag_clssa_clssa_d,H"
peak_mag_above_avg_fn="peak_mag_above_avg_clssa_clssa_d,H"
peak_freq_fn="peak_freq_clssa_clssa_d,H"
peak_phase_fn="peak_phase_clssa_clssa_d,H"
mean_freq_fn="mean_freq_clssa_clssa_d,H"
rtm_mag_fn="rtm_mag_clssa_clssa_d,H"
bandwidth_fn="bandwidth_clssa_clssa_d,H"
slope_fn="slope_clssa_clssa_d,H"
roughness_fn="roughness_clssa_clssa_d,H"
unique_project_name="clssa"
suffix="d"
f1=5
f2=10
f3=120
f4=140
df_out=2
win_len=40
n_iter=2
alpha=0.001
residue_threshold=5
want_peak_attr=y
want_spectral_mag=y
want_spectral_phase=n
want_phase_residue=n
want_reconstructed_data=n
want_4d_cubes=y
use_mpi=y
processors_per_node=16
node_list="localhost"
verbose=n
first_line_out=105
last_line_out=201
first_cdp_out=74
last_cdp_out=206
[li2189@tripolite boonsville]$
```

The file in your working directory will always take precedence over the one in the `/${AASPIHOME}/scripts` directory.

As in all the AASPI GUIs, click *Execute* to run the program. The end of your run should look something like the following:

Spectral Attributes: Program **spec_clssa**

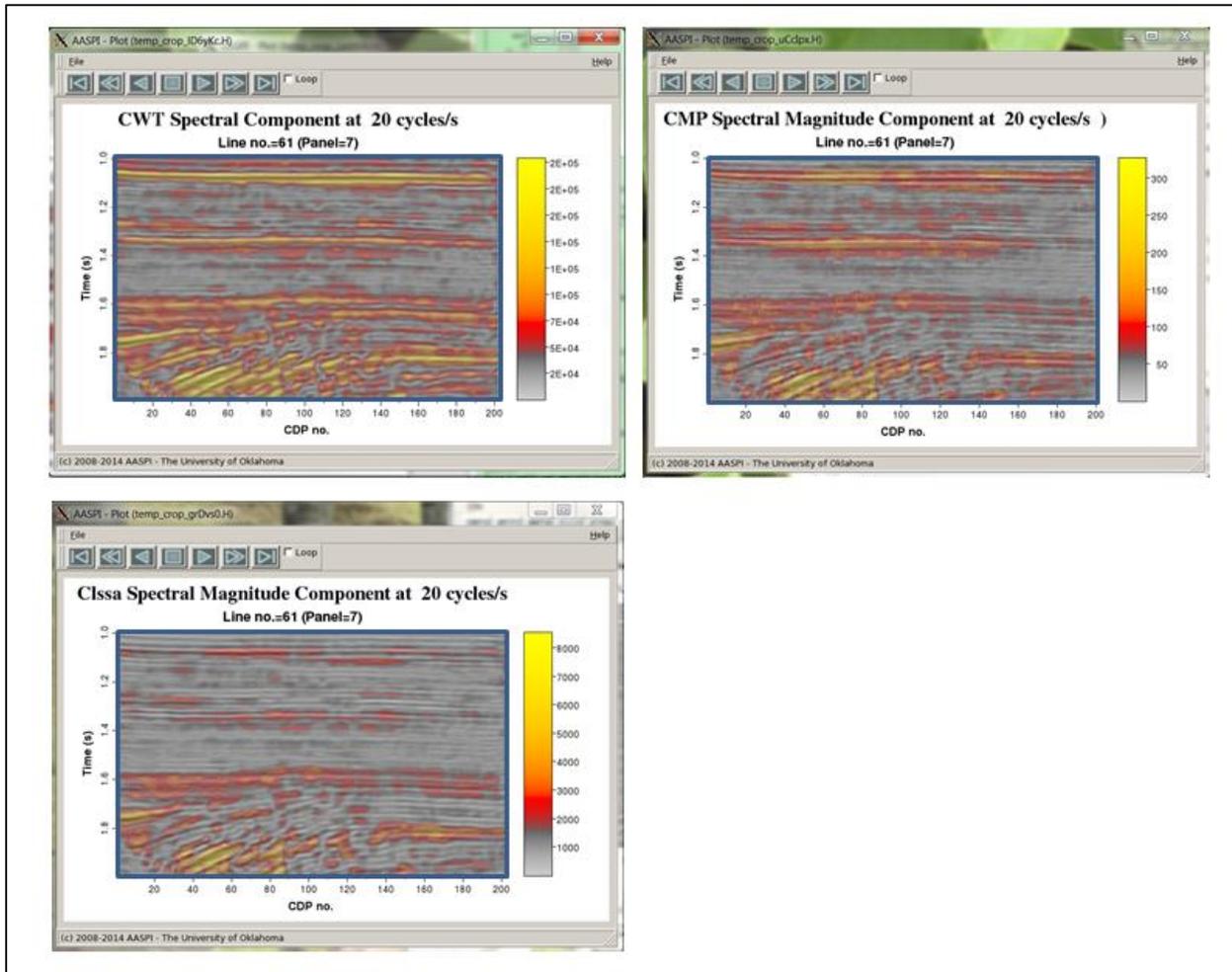


```
li2189@tripolite:/raid5/li2189/boonsville
0: begin_line_out,jline,end_line_out      1    95    97
0: begin_line_out,jline,end_line_out      1    96    97
0: begin_line_out,jline,end_line_out      1    97    97
 3 :normal completion,routine: spec_clssa
 4 :normal completion,routine: spec_clssa
 5 :normal completion,routine: spec_clssa
 7 :normal completion,routine: spec_clssa
15 :normal completion,routine: spec_clssa
 6 :normal completion,routine: spec_clssa
 9 :normal completion,routine: spec_clssa
11 :normal completion,routine: spec_clssa
13 :normal completion,routine: spec_clssa
10 :normal completion,routine: spec_clssa
12 :normal completion,routine: spec_clssa
14 :normal completion,routine: spec_clssa
 8 :normal completion,routine: spec_clssa
16 :normal completion,routine: spec_clssa
 0 :normal completion,routine: spec_clssa
Closing file: /nfs/raid5/li2189/boonsville/d_mig_boonsville.H
Closing file: mean_freq_clssa_clssa_d,H
 1 :normal completion,routine: spec_clssa
Closing file: peak_freq_clssa_clssa_d,H
Closing file: peak_mag_clssa_clssa_d,H
Closing file: peak_phase_clssa_clssa_d,H
Closing file: spec_mag_4d_clssa_clssa_d,H
 2 :normal completion,routine: spec_clssa
```

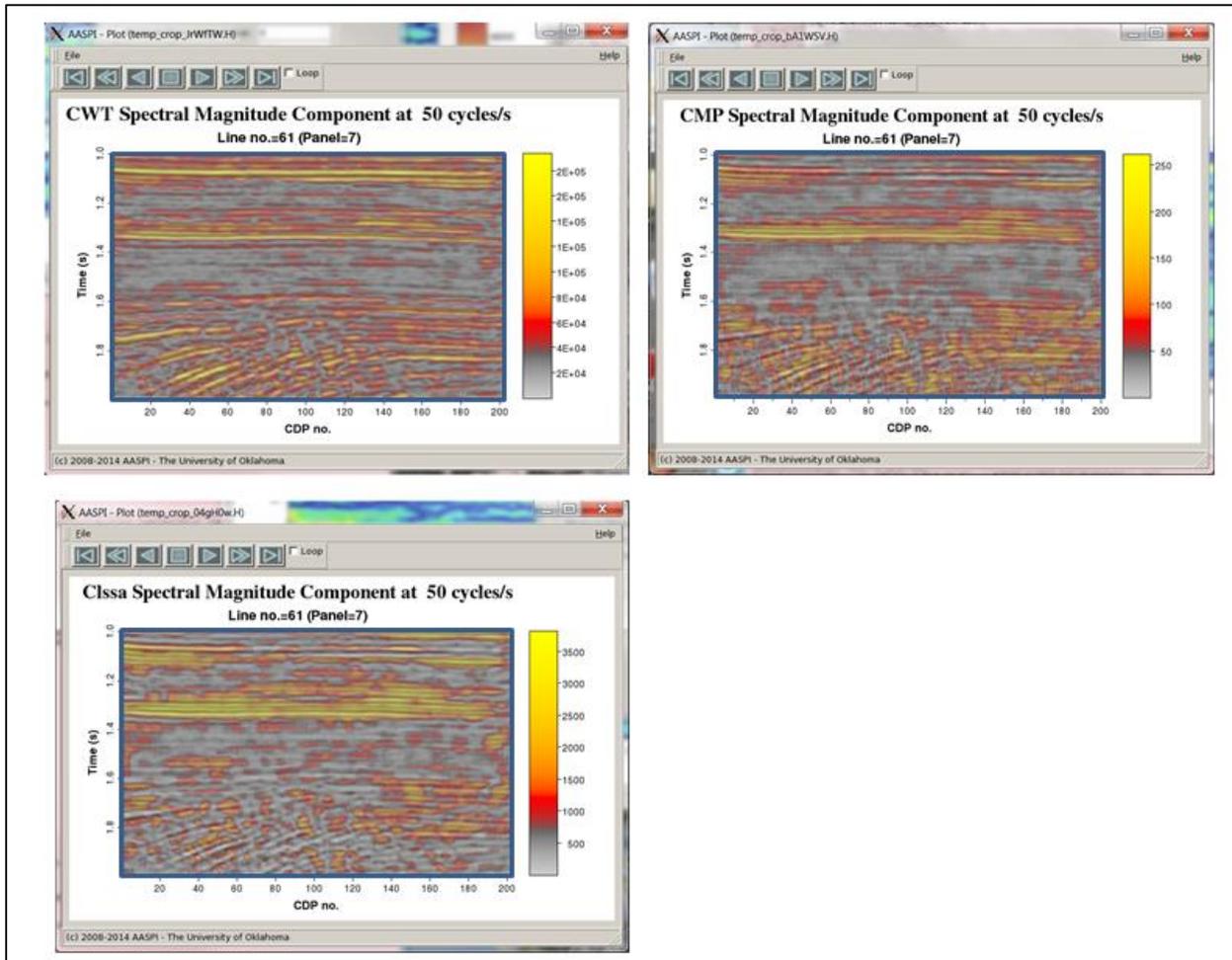
Example 1: Comparison of the three decomposition algorithms

Our first example compares vertical slices of spectral components at 20 Hz and 50 Hz through the UT BEG Stratton data volume. Note that 20 Hz has a period of 0.050 s which is larger than the 0.040 s analysis window used in **spec_clssa**. The 20 Hz component from **spec_cwt** is not really a component, but rather the relatively broad band response of a Morlet wavelet centered at 20 Hz, with a Gaussian spectrum with half power = f . The 20 Hz component from **spec_cmp** is the complex sum of all 20 Hz components of Morlet wavelets about a given time sample. For this reason, both **spec_clssa** and **spec_cmp** have higher frequency resolution than **spec_cwt**.

Spectral Attributes: Program **spec_clssa**



Spectral Attributes: Program `spec_clssa`

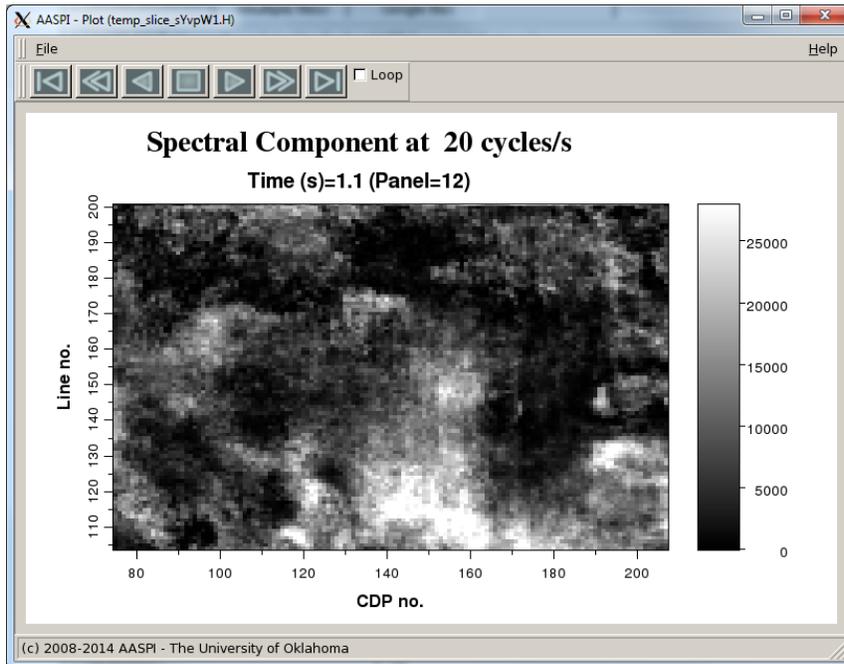


Example 2: `clssa` applied to the Boonsville survey

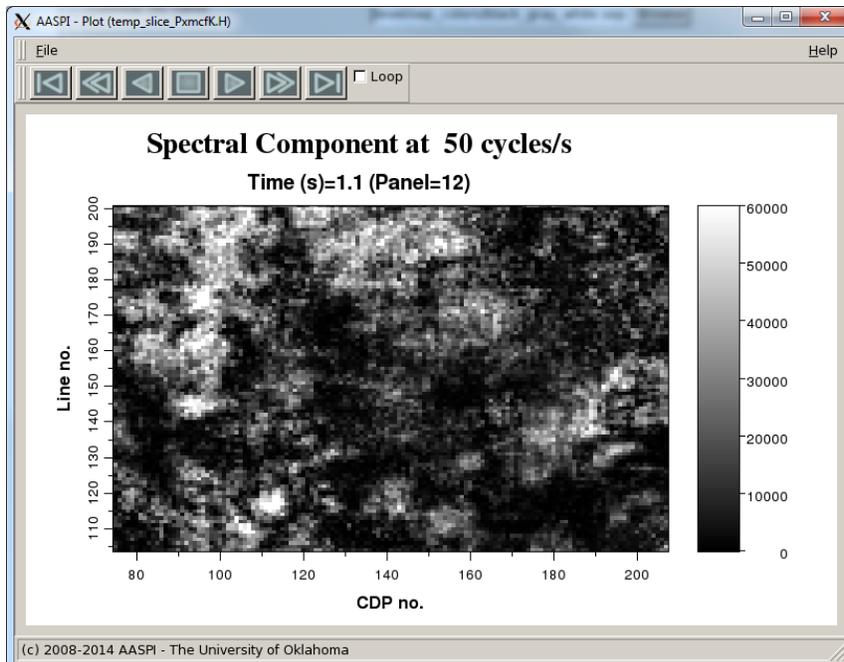
Now, plot some of the results. Since we did not choose to store the spectral magnitude and phase components as a 4D cubes, we have several 3D volumes we can plot separately.

Plotting the same time slice as in all the other examples, and setting `Allpos=y` in our SEP Viewer GUI for the strictly positive magnitude, the `spec_mag_3d_clssa_d_20.H` (the 20 Hz magnitude component) file looks like this:

Spectral Attributes: Program `spec_clssa`

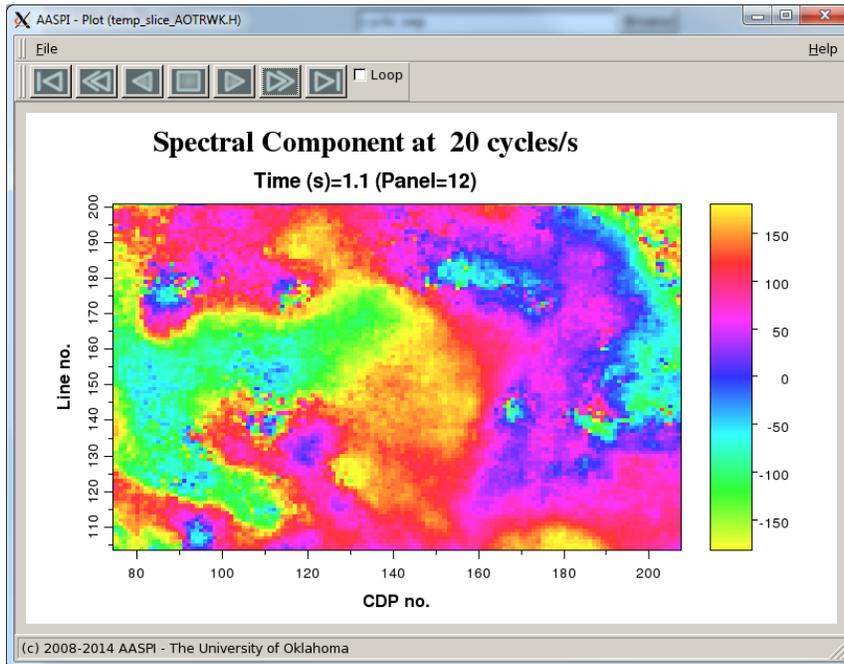


While the `spec_mag_3d_clssa_d_50.H` (the 50 Hz magnitude component) file looks like this:

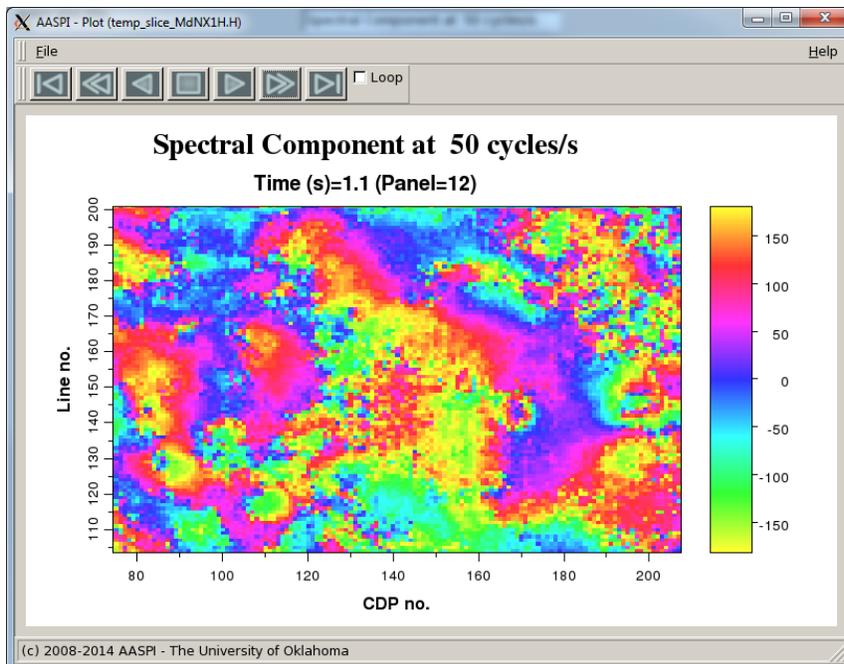


The phase components will range from -180° to $+180^{\circ}$, so set `Allpos=n` and choose a cyclical color bar to plot `spec_phase_3d_clssa_d_20.H` (the 20 Hz phase component):

Spectral Attributes: Program `spec_clssa`

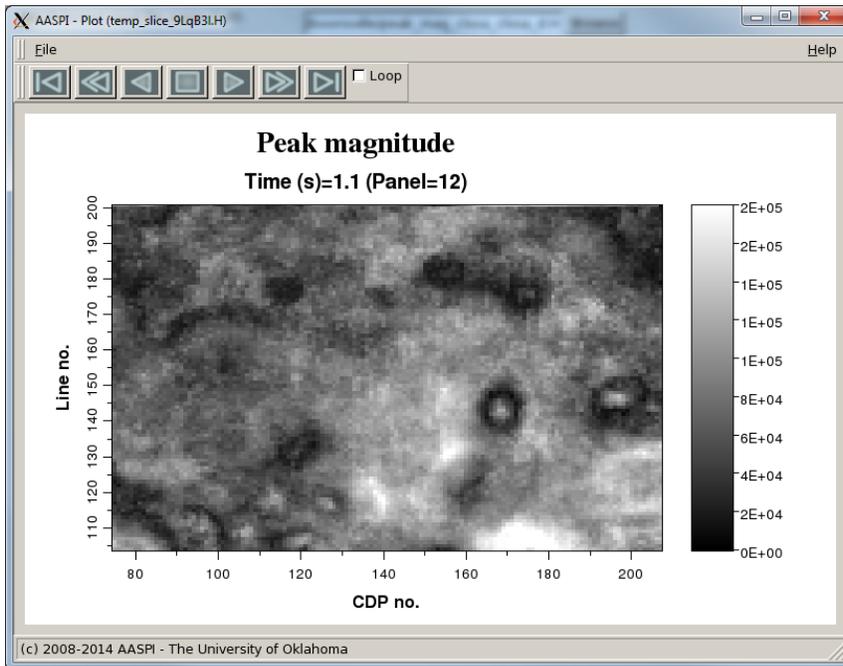


and `spec_phase_3d_clssa_d_50.H` (the 50 Hz phase component):

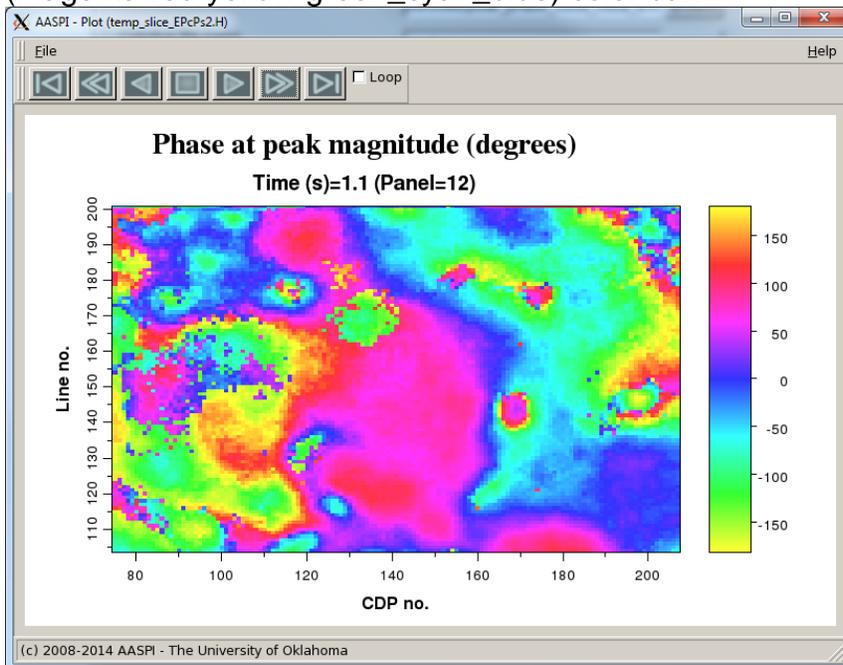


Several measures of the spectrum at each time sample are also computed. The simplest one is the peak magnitude (the greatest value of the spectrum) here as the file `peak_magnitude_clssa_d.H`:

Spectral Attributes: Program `spec_clssa`



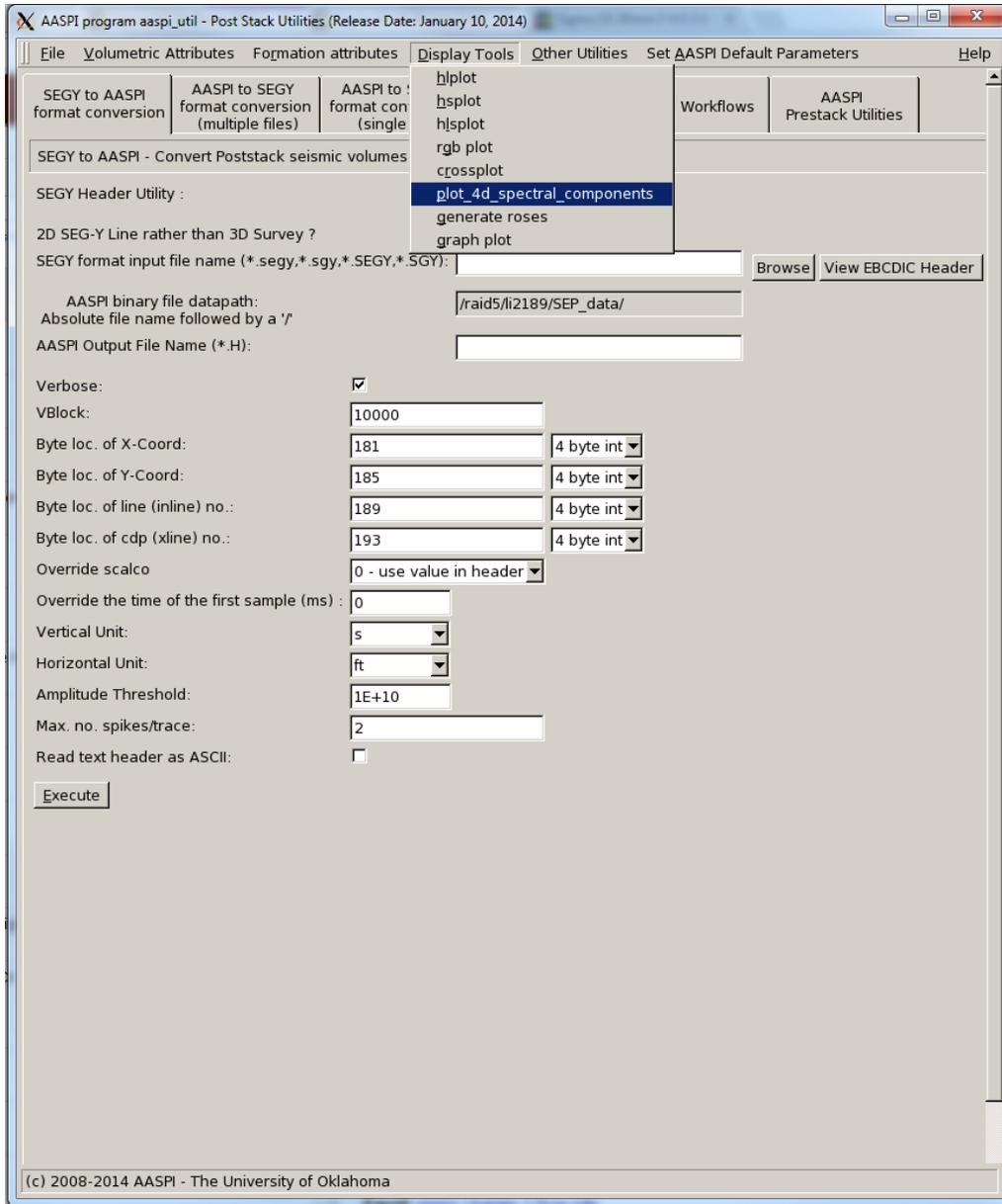
We can also plot the corresponding frequency at this value (the peak frequency) which for this case is the *file peak_freq_3d_clssa_d.H* plotted against the *frequency.sep* (magenta-red-yellow-green-cyan-blue) color bar:



Plotting Spectral Components

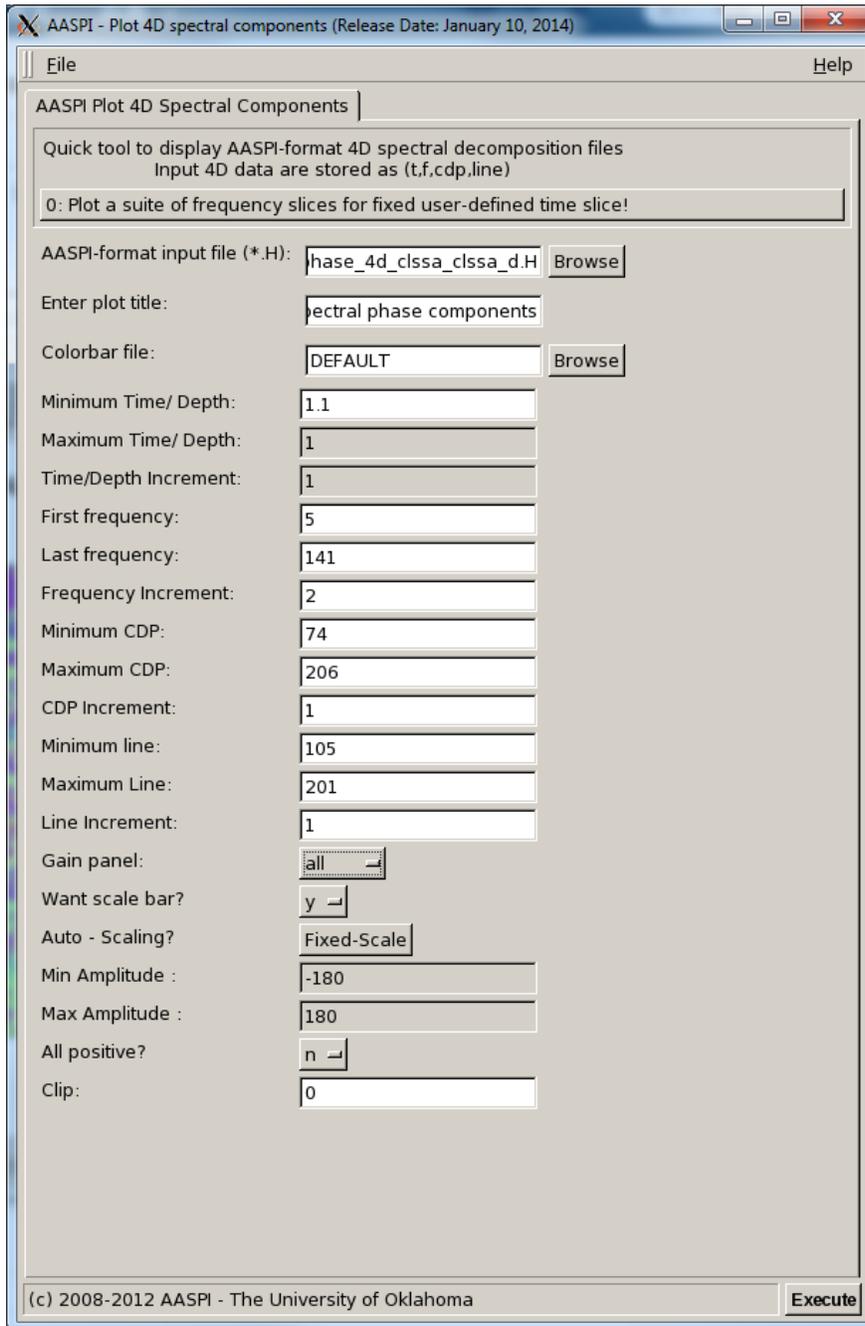
Spectral Attributes: Program `spec_clssa`

We provide a simple graphical interface to quality control the spectral components. Many commercial workstation software products now provide excellent interactive visualization of 4D volumes (t , x , y , and typically offset h , but in our case frequency, f). Our crude tool `plot_4D_spectral_components` can be found under the *Display tools* tab:



Previously, I had computed spectral components for the Boonsville survey and stored them as a 4D volume ($t, f, line_no, cdp_no$) in a file `spec_phase_4d_clssa_d_0.H`

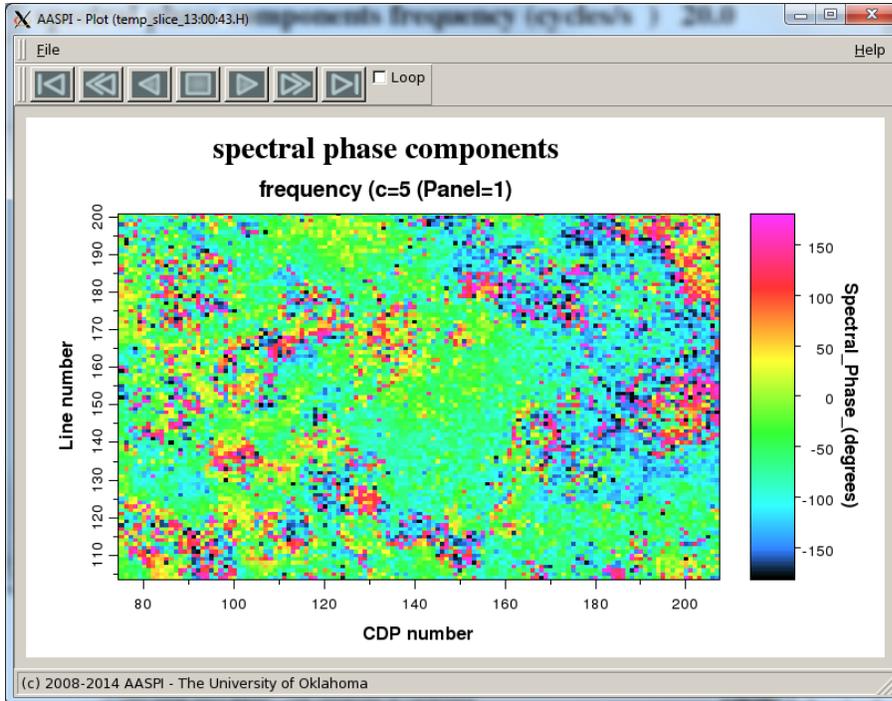
Spectral Attributes: Program `spec_clssa`



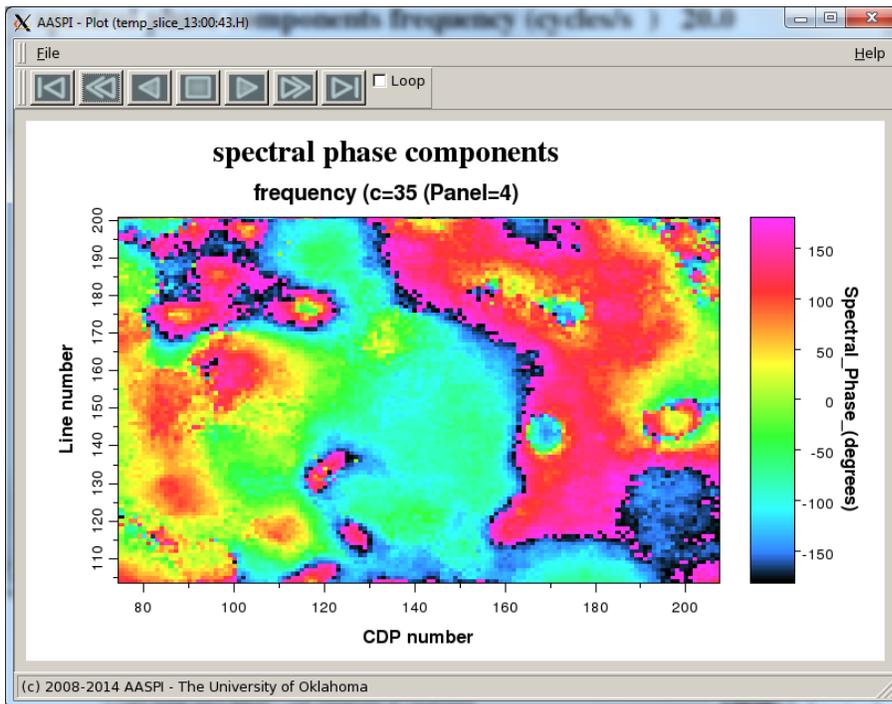
The upper selection bar allows me to plot a constant frequency section or a constant time section. I've chosen the 1.1s time slice. I choose the *energy.sep* color bar and obtain these slices of different frequencies at 1.1s time slice:

Spectral Attributes: Program `spec_clssa`

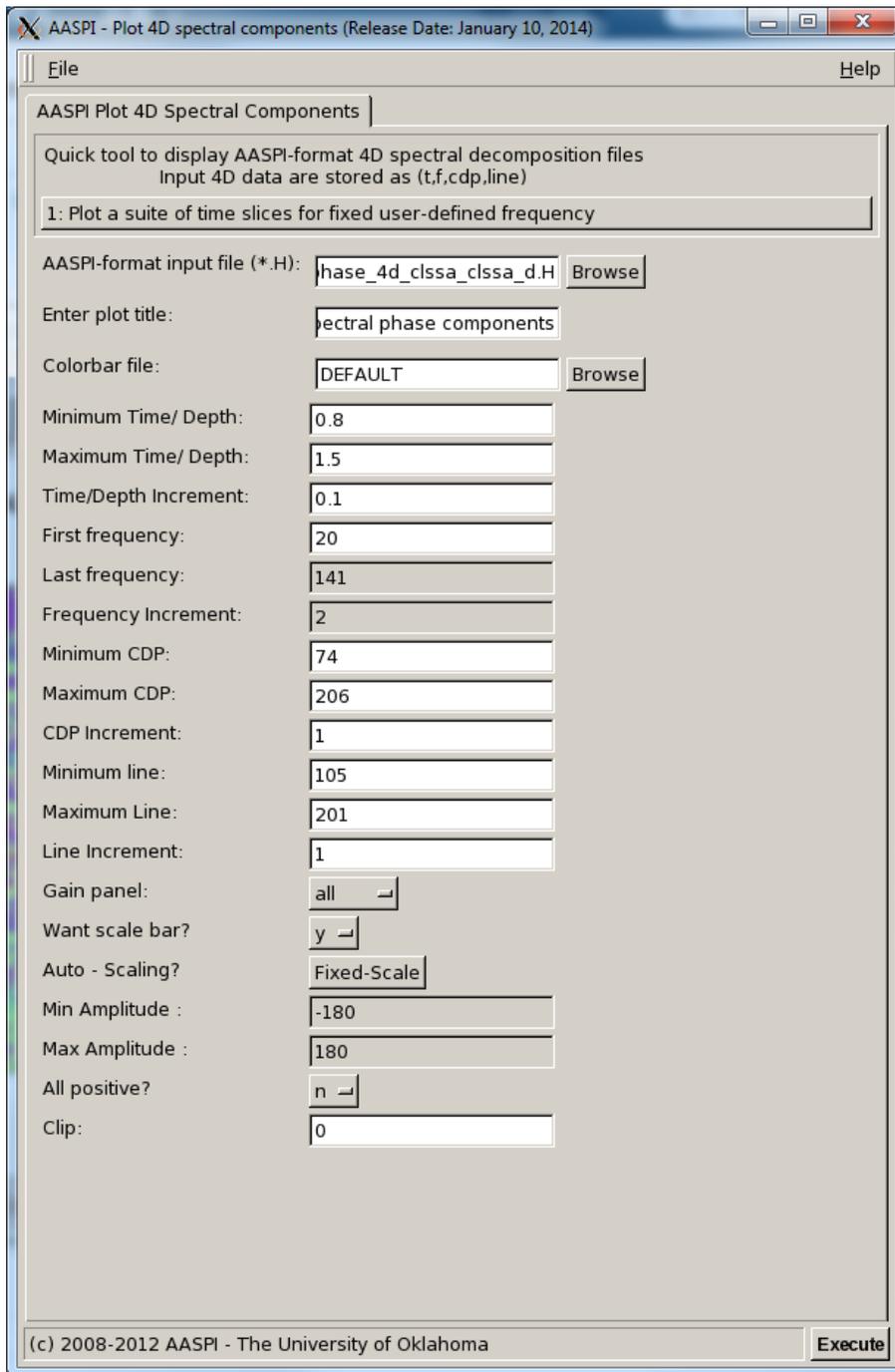
First, 5 Hz component at 1.1s:



Then, 35 Hz component at 1.1s:



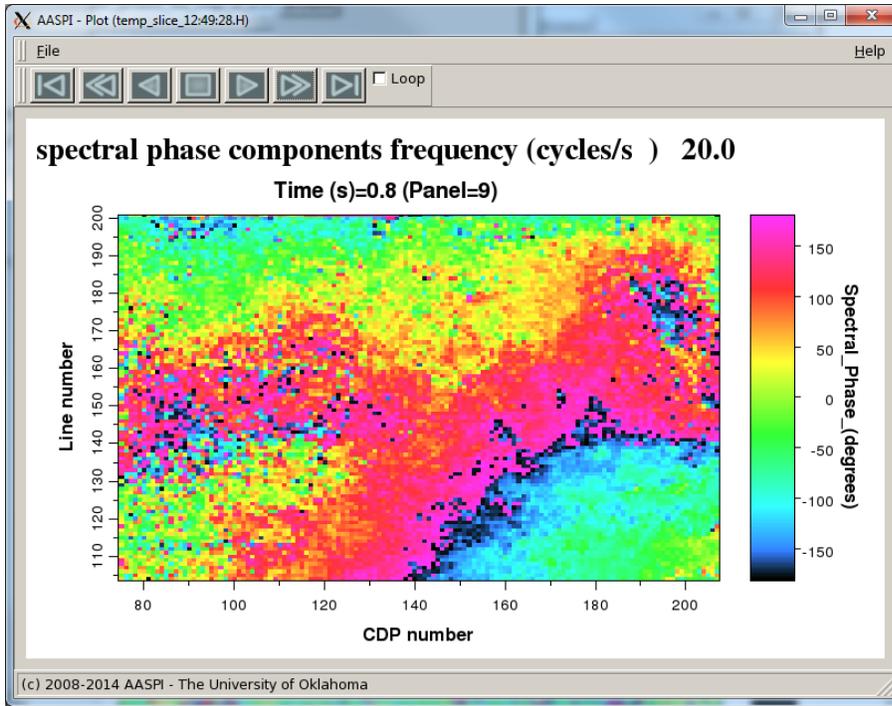
Spectral Attributes: Program `spec_clssa`



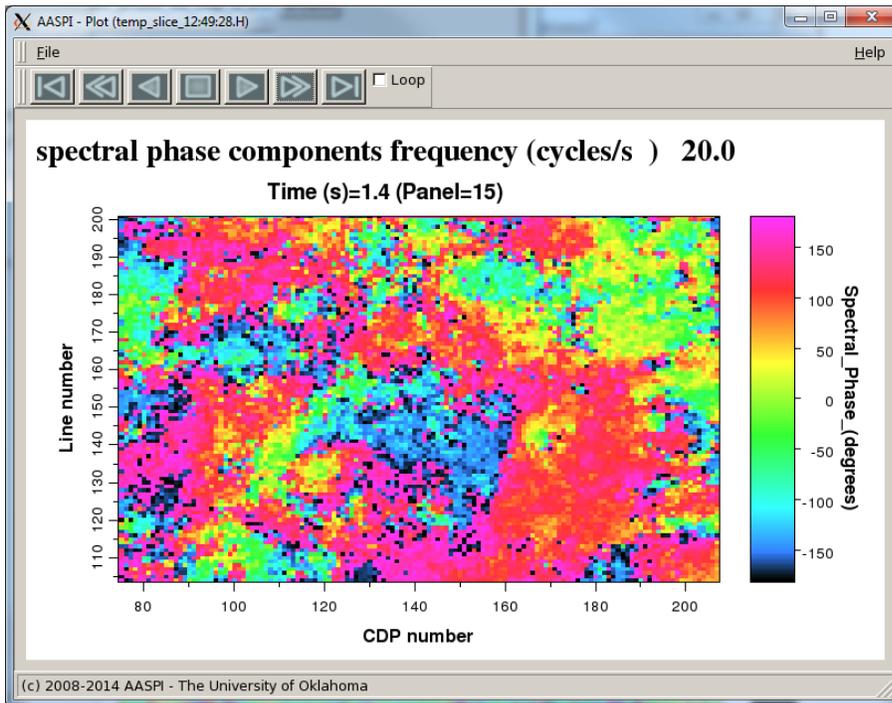
The upper selection bar allows me to plot a constant frequency section or a constant time section. I've chosen the 20 Hz component. I choose the *energy.sep* color bar and obtain these time slice through a 20 Hz volume:

Spectral Attributes: Program `spec_clssa`

First, 0.8s time slice of 20 Hz component:

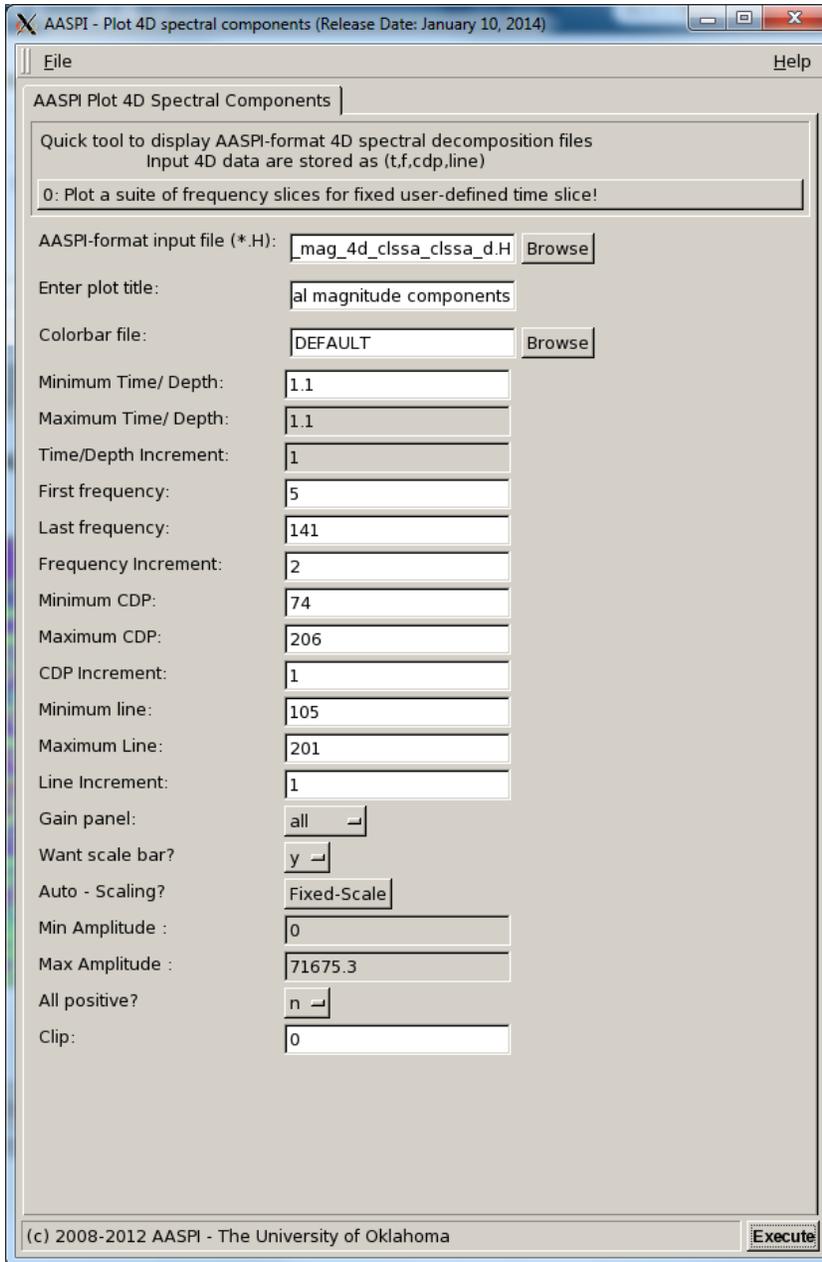


Then, 1.4s time slice of 20 Hz component:



Spectral Attributes: Program `spec_clssa`

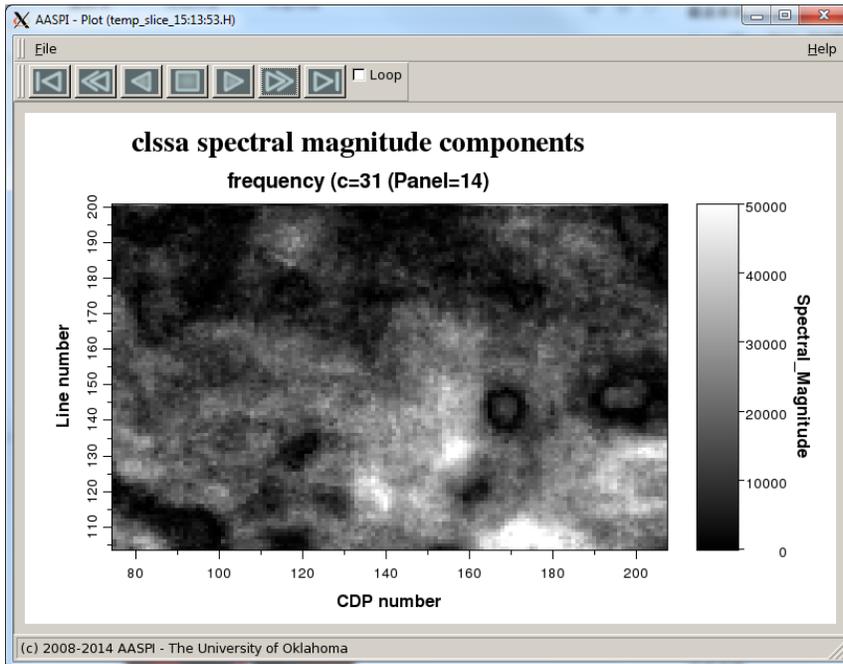
I can also generate similar plots of the `spec_mag_4d_clssa_0.H` 4D volume.



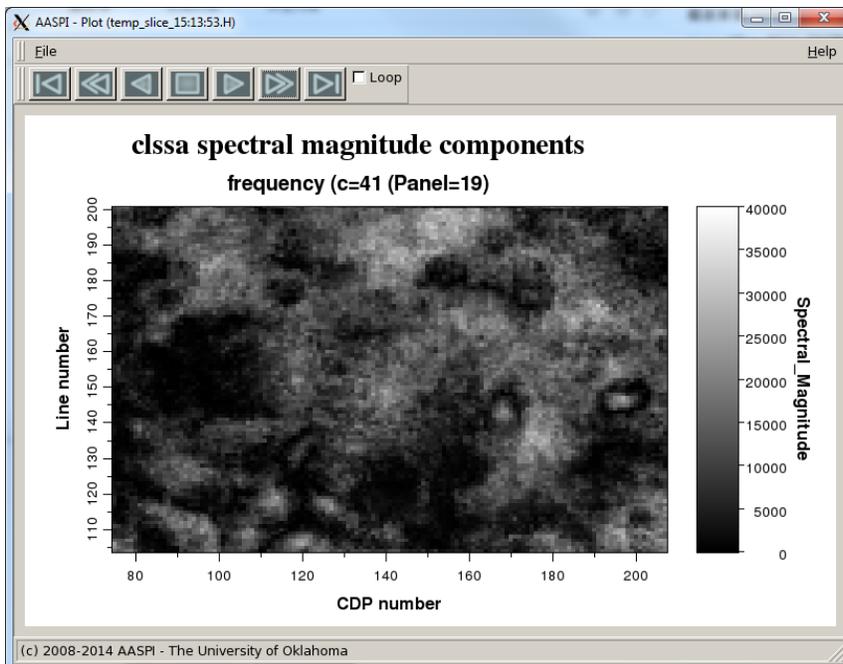
I display the 31 Hz and 41 Hz spectral magnitude slices at 1.1 s:

First, 31 Hz spectral magnitude slices at 1.1 s:

Spectral Attributes: Program `spec_clssa`



Then, 41 Hz spectral magnitude slices at 1.1 s:



References

Spectral Attributes: Program **spec_clssa**

Portniaguine, O., and J. P. Castagna, 2004, Inverse spectral decomposition: 74th Annual International Meeting, SEG, Expanded Abstracts, 1786–1789.

Purveyer C. I., O. N. Portniaguine, C. M. Cobos, and J. P. Castagna, 2012, Constrained least-squares spectral analysis: Application to seismic data. *Geophysics*, **77**, V143–V167.