

# Target-oriented thin-bed prediction using spectral inversion Bin Lyu, Marcílio Castro de Matos, Jie Qi, Ying Hu and Kurt J. Marfurt, University of Oklahoma





reflectivity  $r_1$  and  $r_2$ , the Green function centered at time t of thickness  $\Delta t$ ,

$$G(f,\Delta t) = r_1 \exp\left[i2\pi f\left(t - \frac{\Delta t}{2}\right)\right] + r_2 \exp\left[i2\pi f\left(t + \frac{\Delta t}{2}\right)\right]$$

The spectral magnitude is expressed by

$$a(f) = \left| r_1 \exp\left[i2\pi f\left(t - \frac{\Delta t}{2}\right)\right] + r_2 \exp\left[i2\pi f\left(t + \frac{\Delta t}{2}\right)\right] \right|$$

$$\cos(\pi f \Delta t) = \frac{\exp(i\pi f \Delta t) + \exp(-i\pi f \Delta t)}{2}$$
$$\sin(\pi f \Delta t) = \frac{\exp(i\pi f \Delta t) - \exp(-i\pi f \Delta t)}{2}$$

Puryear and Castagna (2008) define the even and odd coefficients,

$\begin{pmatrix} r_{\rm even} \\ r_{\rm odd} \end{pmatrix} =$	$ \left(\begin{array}{c} \frac{1}{2}\\ \frac{1}{2} \end{array}\right) $	$ \begin{bmatrix} \frac{1}{2} \\ -\frac{1}{2} \end{bmatrix} \begin{pmatrix} r_1 \\ r_2 \end{pmatrix} $	or	$\begin{pmatrix} r_1 \\ r_2 \end{pmatrix} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$	$\begin{array}{c}1\\-1\end{array} \begin{pmatrix} r_{\text{even}}\\r_{\text{odd}} \end{pmatrix}$
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Then the Green function can be rewritten as

 $G(f,\Delta t) = 2r_{\text{even}}\cos\left(\pi f\Delta t\right) + i2r_{\text{odd}}\sin\left(\pi f\Delta t\right)$ 

A least-squares method is used to predict the thin-bed thickness, which try to minimize the difference between the observed and modeled spectra using the objective function

 $\min_{r_1,r_2} E^2(\Delta t) = \left\| U(f) - W(f) \left\{ r_1 \exp\left[i2\pi f\left(t - \frac{\Delta t}{2}\right)\right] + r_2 \exp\left[i2\pi f\left(t + \frac{\Delta t}{2}\right)\right] \right\} \right\|^2$ 

### 2019 workplan

In 2019, we will extend this thin-bed spectral inversion method to the application of well property interpolation between nearby wells. A suite of reflectivity models could be generated using the method, followed by comparison to the measured spectra. The model whose spectra best fits the measured one is the "winner", and provides the output "inverted" results from a suite of possible input models. It could also be expanded to be more geostatistical if necessary.

### Conclusions

To address the limitations of the thin-bed thickness estimation method using only peak frequency after spectral decomposition, we developed a spectral inversion method using a leastsquares fitting algorithm, to yield more accurate and stable thickness determinations below tuning. Next, we will focus on extending this method to combine with the well-log data, to improve the vertical resolution, and apply it on well property interpolation and impedance inversion.

## Acknowledgements

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For a given two-layer model with top and bottom The solution of the reflectivity is given by

$$\begin{pmatrix} r_1 \\ r_2 \end{pmatrix} = \left( \mathbf{A}^{\mathrm{T}} \mathbf{A} \right)^{-1} \mathbf{A}^{\mathrm{T}} \begin{pmatrix} U_1 \\ U_2 \\ \vdots \\ U_N \end{pmatrix}$$

The term  $(\mathbf{A}^{T}\mathbf{A})^{-1}\mathbf{A}^{T}$  can be precomputed, where

$$\mathbf{A} = \begin{pmatrix} W(f_1)\exp(+i\pi f_1\Delta t) & W(f_1)\exp(-i\pi f_1\Delta t) \\ W(f_2)\exp(+i\pi f_2\Delta t) & W(f_2)\exp(-i\pi f_2\Delta t) \\ \vdots & \vdots \\ W(f_N)\exp(+i\pi f_N\Delta t) & W(f_N)\exp(-i\pi f_N\Delta t) \end{pmatrix}$$

The tuning thickness is provided by

$$\Delta t_{\text{tuning}} = \arg \left\{ \min_{\Delta t} \left[ E^2 \left( \Delta t \right) \right] \right\}^2$$

The objective functions from cross-correlation analysis indicate effectiveness of the method.



Figure 7. Objective function of synthetic thin-bed model with different thickness: (a) 4ms, (b) 8ms, (c) 16ms, and (d) 24ms.